



Digital Media Laboratory
Sharif University of Technology

Statistical Pattern Recognition

Classification: Introduction & Quality assessment

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<http://ce.sharif.edu/courses/90-91/2/ce725-1/>

Agenda

- ✧ **Introduction**
- ✧ **Classification: A Two-Step Process**
- ✧ **Evaluating Classification Methods**
- ✧ **Classifier Performance**
- ✧ **Performance Measures**
- ✧ **Partitioning Methods**



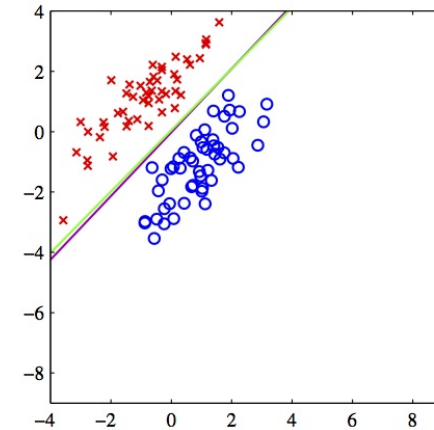
Introduction

✧ Classification

- ✧ predicts categorical class labels (discrete or nominal)
- ✧ classifies data (constructs a model), based on the training set and the class labels, and uses it in classifying new data

✧ Typical applications

- ✧ Credit approval
- ✧ Target marketing
- ✧ Medical diagnosis
- ✧ Fraud detection



Classification: A two-step process

✧ **Model construction**

- ✧ **Each sample is assumed to belong to a predefined class, as determined by the class label**
- ✧ **The set of samples used for model construction is called “training set”**
- ✧ **The model is represented as classification rules, decision trees, probabilistic model, mathematical formulae and etc.**

✧ **Model usage**

- ✧ **for classifying future or unknown objects**
- ✧ **Estimate accuracy of the model**
 - ✧ The known label of test sample is compared with the classified result from the model
 - ✧ Accuracy rate is the percentage of test set samples that are correctly classified by the model
 - ✧ Test set is independent of training set, otherwise over-fitting will occur
- ✧ **If the accuracy is acceptable, use the model to classify data samples whose class labels are not known**



Evaluating classification methods

✧ Performance

✧ classifier performance: predicting class label

- ✧ Accuracy, {true positive, true negative}, {false positive, false negative}, ...

✧ Time Complexity

✧ time to construct the model (training time)

- ✧ the model will be constructed once
- ✧ can be large

✧ time to use the model (classification time)

- ✧ must be tolerable
- ✧ need for good data structures

✧ Robustness

- ✧ handling noise and missing values
- ✧ handling incorrect training data



Evaluating classification methods

✧ **Scalability**

- ✧ **efficiency in disk-resident databases**

✧ **Interpretability**

- ✧ **understanding and insight provided by the model**

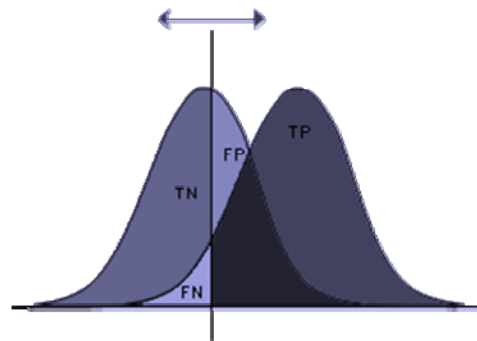
✧ **Other measures: goodness of rules or compactness of classification rules**

- ✧ **rule of thumb: more compact, better generalization**

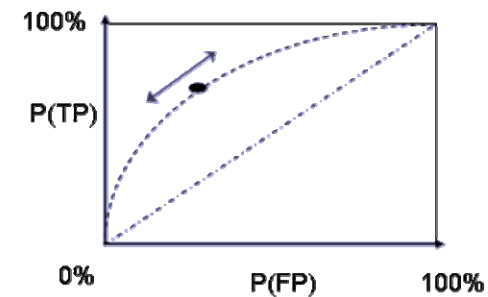


Performance measures

- ✧ Accuracy is not a good measure for classifier performance always (Why?)
 - ✧ Suppose a “cancer detection” problem
- ✧ Presentation of Classifier Performance
 - ✧ Use a confusion matrix or a receiver-operating characteristic (ROC) curve



		Real	
		P	N
Predicted	P	TP	FP
	N	FN	TN



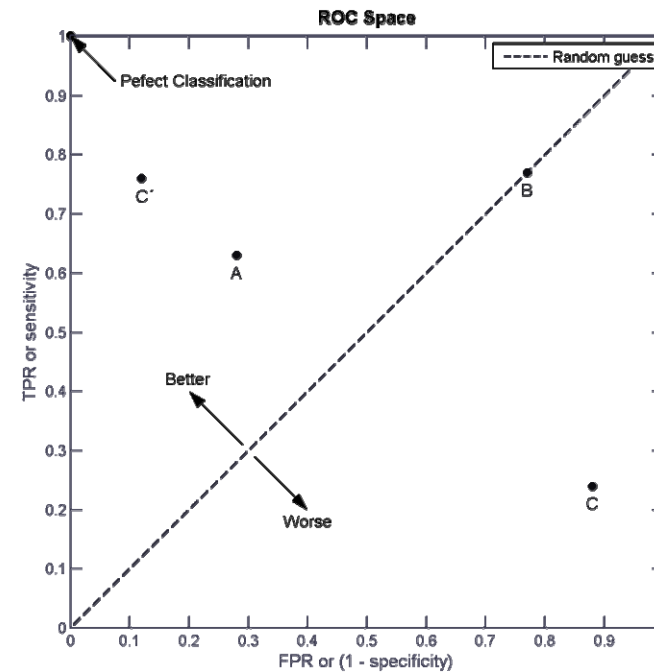
- ✧ We can extract some performance measures from the above matrix (or curve)



Performance measures

✧ ROC Example: ROC Space

✧ A:	<table border="1"><tr><td>TP: 63</td><td>FP: 28</td></tr><tr><td>FN: 37</td><td>TN: 72</td></tr></table>	TP: 63	FP: 28	FN: 37	TN: 72	91 109 100 100 200	Acc: 0.68
TP: 63	FP: 28						
FN: 37	TN: 72						
✧ B:	<table border="1"><tr><td>TP: 77</td><td>FP: 77</td></tr><tr><td>FN: 23</td><td>TN: 23</td></tr></table>	TP: 77	FP: 77	FN: 23	TN: 23	154 46 100 100 200	Acc: 0.50
TP: 77	FP: 77						
FN: 23	TN: 23						
✧ C:	<table border="1"><tr><td>TP: 24</td><td>FP: 88</td></tr><tr><td>FN: 76</td><td>TN: 12</td></tr></table>	TP: 24	FP: 88	FN: 76	TN: 12	112 88 100 100 200	Acc: 0.18
TP: 24	FP: 88						
FN: 76	TN: 12						
✧ C':	<table border="1"><tr><td>TP: 76</td><td>FP: 12</td></tr><tr><td>FN: 24</td><td>TN: 88</td></tr></table>	TP: 76	FP: 12	FN: 24	TN: 88	88 112 100 100 200	Acc: 0.82
TP: 76	FP: 12						
FN: 24	TN: 88						



Template designed by Jafar Muhammad



Performance measures

✧ Performance Measures

- ✧ **Accuracy:** $(TP+TN) / (\#data)$
- ✧ **Specificity:** $TN / (FP+TN)$
- ✧ **Sensitivity:** $TP / (FN+TP)$
- ✧ **Index of Merit:** $(Specificity + Sensitivity) / 2 = (TP\%+TN\%) / 2$
 - ✧ Also known as “percentage correct classifications”

✧ Performance measured using test set results

- ✧ **Test set should be distinct and different from the train (learning) set.**
- ✧ **Several methods are available to partition the data into separated training and testing sets, resulting in different estimates of the “true” index of merit**



Data partitioning

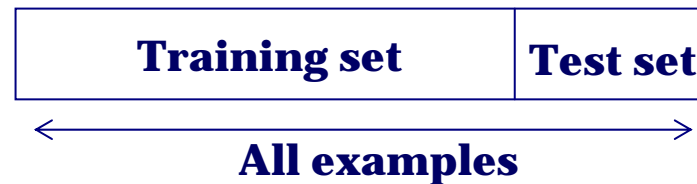
- ✧ **Goal: validating the classifier and its parameters**
 - ✧ **Choose the best parameter set**
- ✧ **Idea: use a part of training data as the validation set**
- ✧ **Validation set must be a good representative for the whole data**
- ✧ **How to partition the training data**



Data partitioning methods

✧ Holdout methods: Random Sampling

- ✧ data is randomly partitioned into two independent sets
- ✧ Always size of train set is twice of test set
- ✧ Assumption: data is uniformly distributed



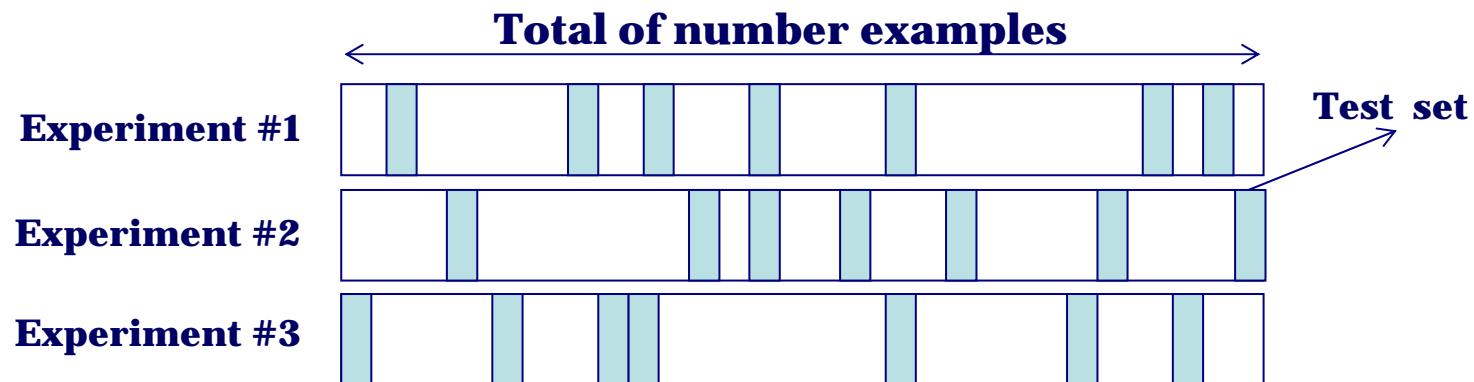
✧ Holdout methods: Bootstrap

- ✧ resample with replacement n sample of original data as training set.
- ✧ Some numbers in the original sample may be included several times in the bootstrap sample (63.2% of samples are distinct)



Data partitioning methods

✧ Holdout methods: Multiple train-and-test experiment Bootstrap



✧ Holdout methods Drawbacks

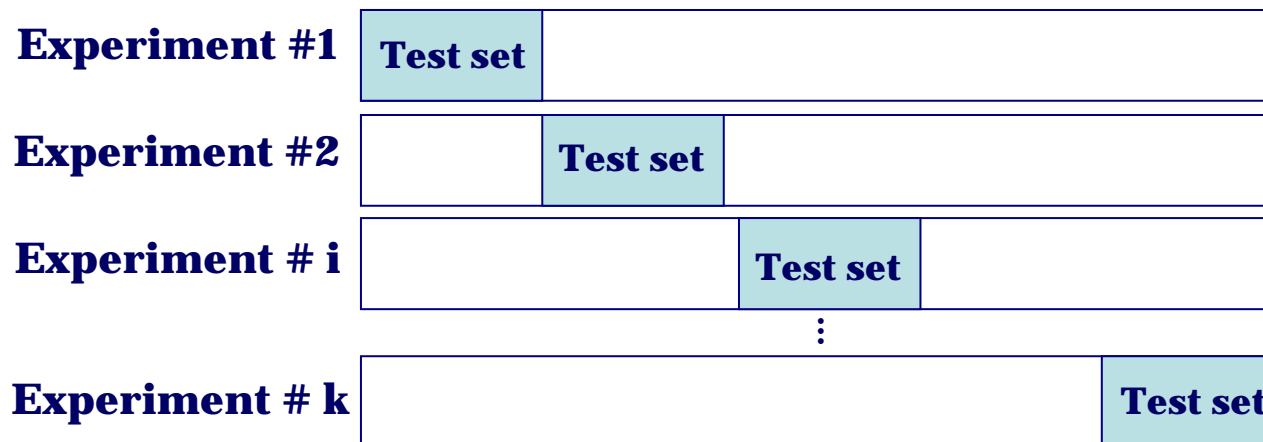
- ✧ In problems where we have a sparse dataset we may not be able to afford the “luxury” of setting aside a portion of the dataset for testing.
- ✧ Since it is a single train-and-test experiment, the holdout estimate of error rate will be misleading if we happen to get an “unfortunate” split.



Data partitioning methods

✧ Cross-validation (k-fold, where $k = 10$ is most popular)

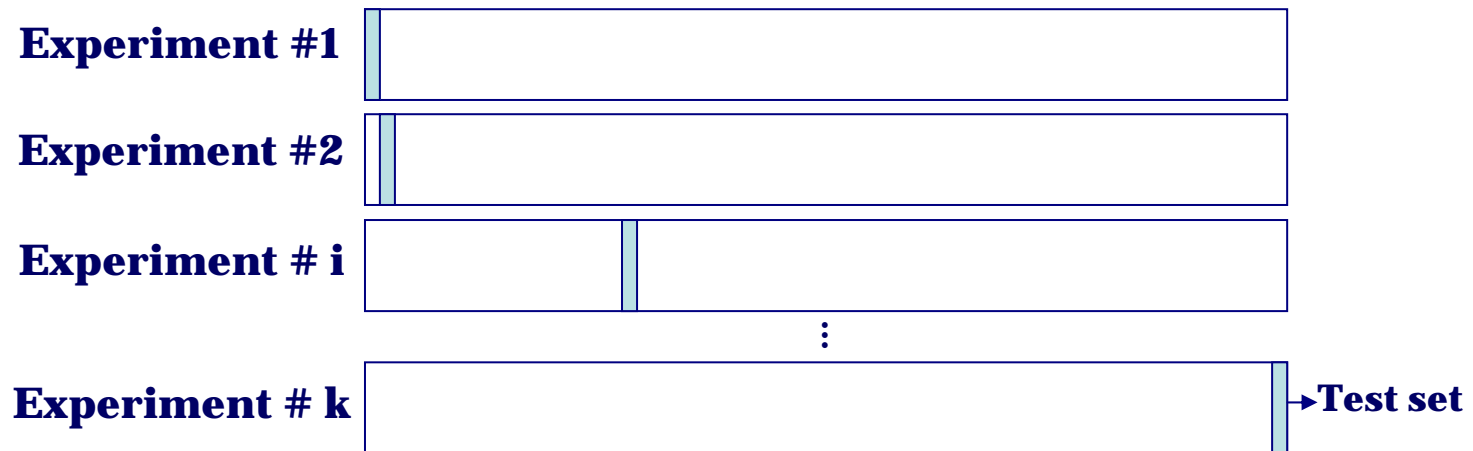
- ✧ Randomly partition the data into k mutually exclusive subsets, each approximately equal size
- ✧ At i^{th} iteration, use D_i as test set and others as training set
- ✧ The mean of measures obtained in iterations used as output performance measure



Data partitioning methods

✧ Leave-one-out

✧ k folds where $k = \#$ of samples, for small sized data



Data partitioning methods

✧ **Stratified cross-validation**

- ✧ **folds are stratified so that class distributions in each fold is approximate the same as that in the initial data**



How many folds are needed?

✧ With a large number of folds

- ✧ + The bias of the true error rate estimator will be small (the estimator will be very accurate)
- ✧ - The variance of the true error rate estimator will be large
- ✧ - The computational time will be very large as well (many experiments)

✧ With small number of folds

- ✧ + The number of experiments and, therefore, computation time are reduced
- ✧ + The variance of the estimator will be small
- ✧ - The bias of the estimator will be large(conservative or higher than the true error rate)

✧ In practice, the choice of the number of folds depends on the size of the dataset

- ✧ For large datasets, even 3-Fold Cross Validation will be quite accurate
- ✧ For very sparse datasets, we may have to use leave-one-out in order to train on as many examples as possible



Three-way data splits

- ✧ **If model selection and true error estimates are to be computed simultaneously, the data needs to be divided into three disjoint sets**
 - ✧ **Training set:** a set of examples used for learning: to fit the parameters of the classifier
 - ✧ **Validation set:** a set of examples used to tune the parameters of a classifier
 - ✧ **Test set:** a set of examples used only to assess the performance of a fully-trained classifier
- ✧ **Why separate test and validation sets?**
 - ✧ The error rate estimate of the final model on validation data will be biased (smaller than the true error rate) since the validation set is used to select the final model
 - ✧ After assessing the final model with the test set, **YOU MUST NOT** tune the model any further



Any Question?

End of Lecture 5

Thank you!

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